The study of the universe at energies above 100 GeV is a relatively new and exciting field. The current generation of pointed instruments have detected TeV gamma rays from at least 10 sources and the next generation of detectors promises a large increase in sensitivity. We have also seen the development of a new type of all-sky monitor in this energy regime based on water Cherenkov technology (Milagro). To fully understand the universe at these extreme energies requires a highly sensitive detector capable of continuously monitoring the entire overhead sky. Such an instrument could observe prompt emission from gamma-ray bursts and probe the limits of Lorentz invariance at high energies. With sufficient sensitivity it could detect short transients (~15 minutes) from active galaxies and study the time structure of flares at energies unattainable to space-based instruments. Unlike pointed instruments a wide-field instrument can make an unbiased study of all active galaxies and enable many multi-wavelength campaigns to study these objects. This paper describes the design and performance of a next generation water Cherenkov detector. To attain a low energy threshold and have high sensitivity the detector should be located at high altitude (> 4km) and have a large area (~40,000 m²). Such an instrument could detect gamma ray bursts out to a redshift of 1, observe flares from active galaxies as short as 15 minutes in duration, and survey the overhead sky at a level of 50 mCrab in one year.

I. INTRODUCTION

The past 15 years have seen large advances in the capabilities of ground-based gamma ray detection, from the pioneering observation of the Crab Nebula by the Whipple observatory in 1989[17] to the new generation of air Cherenkov telescope arrays such as HESS[10], VERITAS[18], and CANGAROO[19] and large area air Cherenkov telescopes such as STACEE[7], CELESTE[14], and MAGIC[13]. There are now at least 10 known sources of very-high-energy (VHE) gamma rays[11]. The physics of these objects is astounding: from spinning neutron stars to super-massive black holes, these objects manage to accelerate particles to energies well in excess of 10 TeV. How this acceleration occurs is not well understood and there is not universal agreement on what particles are being accelerated in some of these sources. At lower energies EGRET has detected over 270 sources of high-energy gamma rays[8] and GLAST is expected to detect several thousand sources. In addition there are transient sources such as gamma-ray bursts that have to date eluded conclusive detection in the VHE regime (despite some tantalizing hints[4]). The paucity of VHE sources can be traced to the nature of the existing instruments: they are either narrow field instruments that can only view a small region of the sky at any one time and can only operate on clear moonless nights (Whipple, HEGRA, etc.) or large field instruments with limited sensitivity (Milagro, Tibet Array).

The Milagro observatory has pioneered the use of a large area water Cherenkov detector for the detection of extensive air showers. Since an extensive air shower (EAS) array directly detects the particles that survive to ground level it can operate continuously and simultaneously view the entire overhead sky. With the observation of the Crab Nebula and the active galaxies Mrk 421 and Mrk 501, Milagro has proven the efficacy of the technique and its ability to reject the cosmic-ray background at a level sufficient to detect sources[5]. At the same time the Tibet group[3] has demonstrated the importance of a high-altitude site and what can be accomplished with a classical scintillator array at extreme altitudes.

A detector with the all-sky and high-duty factor capabilities of Milagro, but with a substantially lower energy
threshold and a greatly increased sensitivity, would dramatically improve our knowledge of the VHE universe. Reasonable design goals for such an instrument are:

- Ability to detect gamma-ray bursts to a redshift of 1.0
- Ability to detect AGN to a redshift beyond 0.3
- Ability to resolve AGN flares at the intensities and durations observed by the current generation of ACTs
- Ability to detect the Crab Nebula in a single transit

This paper describes a design for a next generation all-sky VHE gamma-ray telescope, the HAWC (High Altitude Water Cherenkov) array, that satisfies these requirements. To quantify the definition of observing “short” flares from AGN, previous measurements of flare intensities and durations by air Cherenkov telescopes can be used. To date the shortest observed flares have had \( \sim 15 \) minute durations with an intensity of 3-4 times that of the Crab. The low energy threshold needed to accomplish these goals requires that the detector be placed at extreme altitudes (HAWC would be situated at an altitude of \( \sim 4500 \) meters) and the required sensitivity demands a large area detector - of order \( 40,000 \) m\(^2\). Section II discusses the limiting performance of an EAS array based on the properties of the EAS, section III gives a physical description of the HAWC and section IV details the expected performance of HAWC.

II. PARTICLE DETECTION ARRAYS IN VHE ASTRONOMY

The ultimate performance of an EAS array will be determined by the number, type, position, arrival time, and energy of the particles that reach the ground. Here these properties of air showers are investigated to arrive at the limiting performance of EAS arrays. To attain this level of performance an EAS array would have to measure each of the above parameters with good precision.

The most well-studied aspect of EAS is the dependence of the number of particles to reach ground level on the observation altitude. For electromagnetic cascades, approximation B is a good estimator of the average number of particles in an EAS as a function of atmospheric depth. However, at the threshold of an EAS array, it is the fluctuations in the shower development that determines the response of the detector. To incorporate the effect of shower fluctuations the event generator CORSIKA (version 6.003) is used to generate EAS from gamma rays. The gamma rays were generated with an \( E^{-2.4} \) spectrum beginning at 10 GeV, and uniformly over over the sky with zenith angles from 0 to 45 degrees. Four different observation altitudes were studied: 2500m, 3500m, 4500m, and 5200m.

Figure I shows the fraction of primary gamma rays that generated an air shower where more than 100 particles with energy above 10 MeV survived to the observation level. The requirement that a particle have at least 10 MeV in energy is imposed as a reasonable detection criterion and the requirement that 100 such particles survive enables one to examine the effects of altitude on the fluctuation spectrum of the air showers. This figure is a reasonable indication of the relative effective area of a fixed detector design as a function of the altitude of the detector. At high energies each km in altitude results in a factor of 2-3 increase in effective area. At low energies (of relevance for extragalactic sources such as GRBs) the increase with altitude is larger. Note that for primary energies between 100 GeV and 500 GeV a detector placed at 5200m has \( \sim 50 \) times more effective area than the identical detector placed at 2500m altitude (close to the altitude of Milagro). From this figure alone one can estimate that a detector roughly 10 times the size of Milagro placed at 5200m altitude would be of order 22 (\( \sqrt{50 \times 10} \)) times more sensitive than Milagro (assuming the background scaled in a similar fashion). This level of sensitivity satisfies the requirements listed above.

It is well known that gamma rays outnumber electrons and positrons in an air shower by a large factor. Figure 2 shows the ratio of gamma rays to electrons (>10 MeV) for three observation altitudes: 3500m, 4500m, and 5200m. Over this altitude range the ratio of gamma rays to electrons is relatively independent of the observation level. At these low energies gamma rays outnumber electrons and positrons by an order of magnitude. Therefore to attain the lowest possible energy threshold the detector must be sensitive to the gamma rays in the air shower.

An important feature of any gamma-ray detector is its ability to reject a significant fraction of the cosmic-ray background. The Milagro detector has demonstrated that detecting and characterizing the penetrating component of an air shower is a reliable method of rejecting the cosmic-ray background. In Figure 3 we show the average number of hadrons and muons in an air shower as a function of primary proton energy. An observation altitude of 5200m is assumed in this figure. It should be noted that the fluctuations about these mean values are not Poisson. But it is clear from this figure that the ability to detect showering hadrons in the air shower is important for the discrimination of the cosmic-ray background. This is especially true at low
energies where the hadronic component is larger than the muon component. (Hadrons are defined to be protons, anti-protons, neutrons, and pions.)

After an event is recorded its direction in the sky must be reconstructed. To establish a limiting angular resolution for an EAS array gamma-ray induced EAS are generated using CORSIKA as above (on an $E^{-2.4}$ spectrum beginning at 10 GeV), however only vertical showers were generated. This simplifies the reconstruction of the air shower. In what follows it is assumed that the position, time, and energy of each particle are measured exactly. Since the direction of the individual particle is not utilized in what follows it may be possible to develop a detector with improved angular resolution, though at a rather large expense. It is beyond the scope of this paper to give a detailed description of the fitting procedure. The leading edge of the EAS is curved: particles farther from the core of the air shower arrive late relative to the particles at the core. Studies of the CORSIKA showers show that this curvature is dependent upon the individual energies of the shower particles. Lower energy particles are delayed longer than higher energy particles. Before using the arrival times of the particles to fit the direction of the primary gamma ray the particle arrival times must be corrected for this effect. To demonstrate the size of this effect Figure 4 shows the point spread function before and after this correction is applied to the particle arrival times (for an observation altitude of 5200m). The median angle error before the
corrections are applied is 5.1 degrees and after the corrections are applied the median angle error is reduced to 0.8 degrees (71% of the events survive the complete fitting procedure). Figure 4 shows the energy dependence of the mean of the point-spread function as a function of primary energy. For a fixed primary energy the angular reconstruction is improved by moving the detector to higher altitude. A detector at 4500m would have the same angular resolution as a detector at 5200m for gamma-ray primaries with 50% more energy. A detector at 3500m altitude would require over a 100% increase in primary energy to obtain a similar angular resolution.

Because of the fluctuations in the shower development (mainly the depth of the first interaction) EAS arrays have relatively poor energy resolution. To investigate the limiting energy resolution of an EAS array primary gamma rays were generated on an $E^{-2.4}$ spectrum from the zenith and the total number of particles with more than 10 MeV that reach the ground within 100m of the shower core were counted. Figure 5 shows the mean (and the error on the mean) number of particles on the ground as a function of primary energy for observation altitudes of 3500m, 4500m, and 5200m. At an altitude of 5200m there is a good correlation between the mean

FIG. 3: The average number of hadrons and muons in an extensive air shower as a function of energy. In this figure an observation altitude of 5200m was assumed.

FIG. 4: The point spread function for the reconstruction of the direction of the primary particle. The angular reconstruction is performed using the actual particle arrival times, positions, and energies. The solid line shows the point spread function after an energy dependent curvature correction is made to the particle arrival times and the dashed line shows the point-spread function before these corrections are made.
number of particles and primary energy at primary energies as low as 50 GeV. At an altitude of 4500m this correlation begins at about 100 GeV in primary energy and at 3500m altitude there is no correlation until the primary energy is about 250 GeV. To estimate the energy resolution, the curves in Figure 5 are fit to a power law in the number of particles that reach the ground ($E = a_0 + a_1 \times N + a_2 \times N^2$, where $N$ is the number of particles on the ground). Figure 6 shows the distribution of $(E_{\text{predicted}} - E_{\text{true}})/E_{\text{true}}$ for primary energies above 50 GeV (for an observation altitude of 5200m). The resulting distribution is non-Gaussian, but is fit reasonably well by a Landau distribution (shown on the figure). The asymmetric tail is an over-estimation of the particle energy and is inherent in the nature of the fluctuations in the depth of the first interaction. With a full width at half maximum of 0.5 the equivalent size of the 1-sigma error bar would be $\sim 25\%$ (if the distribution were Gaussian). As one goes to higher energy primaries the distribution becomes narrower and more Gaussian. At energies below 50 GeV the energy resolution is significantly worse, with an RMS greater than 1. Since the fit is to the mean energy and there is a large positive tail, the peak in the distribution is negative.

This section concludes with a brief summary of the best performance that can be expected from an extensive
air shower array operating at high altitude.

- An energy threshold below 50 GeV
- An angular resolution of 0.25 degrees at median energy
- An energy resolution ∼25% above 50 GeV (with a non-Gaussian tail)

III. DETECTOR DESCRIPTION

Based on the above study and experience with the Milagro detector a complete Monte Carlo simulation of a detector that is similar to Milagro has been performed. The need to detect the gamma rays in the EAS and the penetrating component of muons and hadronic cascades leads to a thick active detector. Water is a natural and inexpensive choice of detecting medium. The Cherenkov photons are relatively plentiful, prompt, and have large mean free paths (relative to the water depth) in clean water. Since the Cherenkov angle in water is 41°, a detector spacing of roughly twice the detector depth ensures that there are no geometrical blind areas. (The depth and spacing were chosen to match that of Milagro, though more work is needed to optimize these parameters.) The choice of a two layer design was again driven by experience with Milagro. The deep layer makes a good calorimeter, whereas a shallow layer does not. In the shallow layer the detected light level depends critically on the exact geometry of the incoming particles, their distance from the photomultiplier tube (PMT) and incident angle. These fluctuations caused by the geometry of the incoming particles dilutes the energy measuring capability of a shallow layer of PMTs. The ability to measure the energy of the shower particles is needed to determine the penetrating component of the air shower. In Milagro this is the most useful method of rejecting the abundant cosmic-ray background. A shallow layer may be required to obtain the best possible angular resolution (also important for rejecting the cosmic-ray background). Since the speed of light in water is substantially different from the speed at which the particles propagate (the speed of light in vacuum), the light and the particles diverge. This leads to an increase in the dispersion of the arrival time of the measured shower front as the depth of the measuring device is increased and the angular resolution is proportional to this spread. This effect is somewhat compensated for by the fact that a deeper layer typically makes more measurements of the shower front (because each PMT can see a larger area of the water surface). The top layer may also be useful in the rejection of the cosmic ray background (described below). Work in better understanding these effects is still underway, but it may be possible to eliminate the shallow layer and maintain the performance of the detector.

In the remainder of this paper, the following detector characteristics are used.

- 40,000m² physical area (200m×200m)
- 2.7m spacing of PMTs (74×74 PMTs per layer)
- Hamamatsu 20cm PMTs (R5912SEL)
- Two layers of PMTs. A shallow layer under 1.5m of water and a deep layer under 6.5m of water
- An attenuation length of 20 meters, composed solely of absorption.
- Trigger requires 50 PMTs in the top layer to be struck by at least 1 photo-electron (PE)
- A detector latitude of 36 degree (that of Milagro)

CORSIKA 6.003 [12] was used to generate the air showers and GEANT 3.21 was used to track the particles through the water, generate the Cherenkov light in the water, and to model the detector response (PMTs, reflectivity of the material, scattering and absorption of light in water, etc.). For the remainder of this paper this design will be referred to as the High Altitude Water Cherenkov (HAWC) array.

IV. DETECTOR PERFORMANCE

A. Event Reconstruction

To obtain realistic estimates of the sensitivity of HAWC, the individual events must be reconstructed - their core position, direction, type (hadronic or gamma ray), and energy need to be determined. Preliminary algorithms have been developed to determine all of these parameters with the exception of the primary energy. Work is ongoing in improving the existing algorithms and developing one to determine the energy of the primary gamma ray. In what follows, the events were generated beginning at 10 GeV on an $E^{-2.49}$ spectrum (similar to that observed for the Crab Nebula [17]) uniformly over incident direction.

As discussed above, the shower front of an EAS is not a true plane. Therefore, the first step in performing an angular reconstruction is the determination of the core of the air shower. A simple center-of-mass algorithm using the pulse heights recorded in the PMTs in the bottom layer of the detector is used to determine the shower core. Figure 8 shows the distribution of core reconstruction errors in meters. For all events that trigger the detector and are successfully reconstructed (see below) the mean core error is 36 meters. Despite the simplicity of the algorithm the core resolution is good enough that it does not degrade the angular resolution. The events with large core errors are those whose cores fall outside of the detector. The dashed line in the figure shows the core error for events whose core falls within the detector, the mean of this distribution is 20 meters.

![Core Error in Meters](image)

**FIG. 8:** The core error in meters using a center-of-mass core algorithm. Gamma ray events with 50 PMTs in the top layer, at least 20 PMTs used in the angular fit are selected. The solid line shows all events and the dashed line contains only events whose core fell inside the array.

The angular reconstruction is performed in an analogous manner to that described above, however the timing correction that was applied based on the individual particle energies is replaced by a correction based upon
the number of PEs measured in each PMT. After applying this correction and a correction for the shower front curvature (proportional to the distance from the PMT to the core of the shower) the resultant times and positions to a plane. In addition the weight associated with each PMT is determined by the measured pulse height. Though the weight also depends upon the distance to the shower core, this effect has been ignored in the following analysis. A 20-30% improvement in the angular resolution may be expected with an improved algorithm. This improvement should arise when the correlations between the two corrections (core distance and pulse height) are utilized and the weights assigned to each PMT incorporate the core distance. The fitting procedure is iterative, where the PMTs that made large contributions to the chi-square are removed in subsequent iterations. Events with more than 20 PMTs surviving in the final iteration of the fitting procedure are considered to be successfully fit. The space angle difference between the true direction and the fit direction is shown in Figure 9. Using this point-spread function the signal to noise ratio is maximal for an analysis bin size of 1.2 degrees. If the point-spread function were Gaussian this bin size would correspond to an angular resolution of 0.75 degrees.

FIG. 9: The space angle difference distribution between the true direction and the fit direction of gamma ray events. This figure includes all gamma rays that triggered the detector and had more than 20 PMTs survive the fitting procedure.

The ability to discriminate between gamma-ray induced air showers and hadronic air showers is critical to the success of any gamma-ray detector. Unlike air Cherenkov telescopes the background rejection discussed here is essentially independent of angular resolution. Based on angular resolution alone with a 2sr field-of-view HAWC (and Milagro) remove roughly 99.93% of the background in their field-of-view. The background rejection discussed below is based purely on differences in the air showers regardless of their incoming direction. Figure 10 shows three gamma-ray induced events and three proton induced events in HAWC. The figure shows the pulse height distribution of the PMTs in the bottom layer of the detector. The area of each square is proportional to the number of detected photoelectrons (PEs) in the PMT. The small black dots represent the PMTs and the square is the position of the shower core. The figure caption gives the primary energy for each event. There are clear differences in morphology between proton and gamma-ray events. Though there are some proton induced events that have a similar morphology to gamma-rays induced events, the events shown here are typical in the sense that most events have similar properties. Note that while some of these events have very low primary energies, they are easily detected in HAWC, striking many PMTs.

Milagro utilizes a parameter known as compactness that is defined as the ratio of the number of PMTs in the bottom layer with more than 2 PEs detected to the maximum number of PEs measured in a single PMT in the bottom layer. Hadronic showers tend to have small values of compactness and gamma ray showers a large value of compactness. The studies performed here indicate that as one moves to higher elevations the ability of this parameter to discriminate between hadronic and gamma-ray initiated cascades degrades. This is consistent with the observations of the Milagro collaboration, who found that the background rejection capabilities of compactness improved as the zenith angle of the primary particle increased. However, a modified form for the compactness parameter, where the number of PMTs with more than 2 PEs is replaced with the number of PMTs that are struck in the bottom layer, has a similar background rejection capability to that obtained by Milagro. Figure 11 shows this modified compactness parameter (which will be referred to simply as compactness in what follows) for proton (dashed line) and gamma ray (solid line) showers. If events are required to have
a compactness greater than 8.3 one retains 66% of the gamma ray events and only 17% of the proton events, yielding a quality factor of 1.6. (The quality factor is defined as the fraction of gamma-ray events that survive the cut divided by the square root of the number of proton events that survive the cut, and is the relative improvement in sensitivity of the detector.)

Another parameter that appears promising in discriminating gamma rays from background is the ratio of the number of PMTs struck in the top layer \((N_{TOP})\) to the number of PEs in the brightest PMT in the bottom layer, where the PMTs within 20m of the fit shower core are excluded from the search for the maximum \((cxE)\). This distribution is shown in Figure 12 for gamma ray and proton induced events. The requirement
$NTOP/cxPE > 2.0$ retains 97.7% of the gamma ray events while rejecting 52.5% of the proton induced events. The important feature of this parameter is that essentially all of the gamma ray events survive, so even though the quality factor is only 1.4 one has retained all of the signal events (regardless of their energy). The requirement $NTOP/cxPE > 4.3$ yields a quality factor of 1.6 (retaining 85% of the gamma ray induced events and 29% of the proton induced events), similar to the compactness criterion, but retaining a larger fraction of the gamma ray events. Unlike the compactness parameter defined above (and that used by Milagro) there is very little energy dependence to this criterion. In Milagro compactness rejects low-energy gamma rays.

FIG. 11: The compactness distribution for proton induced events and gamma-ray induced events.

FIG. 12: The distribution of $NTOP/cxPE$ for proton induced events and gamma-ray induced events. See the text for the definitions of the parameters.

B. Detector Sensitivity

The performance of any detector is determined by its effective area as a function of energy, its angular resolution, the level of the background and the ability to eliminate this background. These considerations can
be parameterized in the following function:

$$S \propto \frac{\int_0^T \sigma(E, \theta) E^{-\alpha} A_g(E, \theta(t))dEdt}{\sqrt{\int_0^T E^{-2.7} A_{cr}(E, \theta(t))dEdt}}$$

(1)

where \( S \) is the “sensitivity” of the detector, \( \sigma(E, \theta) \) is the angular resolution of the detector as a function of energy and zenith angle, \( \alpha \) is the differential spectral index of the source, \( A_g(E, \theta) \) is the effective area of the detector to gamma rays as a function of energy and zenith angle, \( \theta(t) \) is the zenith angle of the source as a function of time, \( A_{cr}(E, \theta) \) is the effective area of the detector to the cosmic-ray background as a function of energy and zenith angle, and \( T \) is the observation time. In determining the functions \( A(E, \theta) \) the background rejection should be included. The time dependence of the zenith angle is required since the energy response of the detector is dependent upon the atmospheric overburden.

To obtain the sensitivity of HAWC, equation (1) is evaluated with the aid of the Monte Carlo. Events are generated on an \( E^{-2.49} \) spectrum for gamma ray primaries and \( E^{-2.7} \) for proton primaries. After following the particles and the Cherenkov light through the detector a list of PMTs that are struck, the number of PE’s in each of these PMTs, and the arrival time of the first PE in each PMT is written to a file. The events are generated over a distribution of zenith angles to mimic an isotropic flux. For a given source declination the time spent at each zenith angle is found and the effective area as a function of energy for that zenith angle is integrated to give a number of detected events as a function zenith angle for a given source declination. Figure 13 shows the effective area as a function of energy for gamma-ray primaries for HAWC at two different detector altitudes, 4572m asl and 5200m asl. The zenith angle averaging in this figure is as if the source was spread uniformly over the sky between zenith angles of 0 and 45 degrees. This figure is used for illustration only. To calculate the sensitivity to a source the integral in equation (1) is evaluated over the source transit (given the declination of the source). In the remainder of the paper (with the exception of the calculation of the sensitivity to gamma-ray bursts) it is assumed that the source is at the declination of the Crab (22 degrees) and the detector is at a latitude of 36 degrees north. Only events that are reconstructed within 1.2 degrees of their true direction are included in the calculation of the effective area. (This accounts for the first term \( \sigma(E, \theta) \) in equation (1)) At high energies (~1 TeV) HAWC at 5200m would have about 170 times the effective area of Milagro to gamma rays and at 100 GeV about 1000 times the effective area of Milagro. As the energy decreases below this, the ratio of effective areas continues to increase, though there are insufficient Monte Carlo events at low energies for Milagro to determine the ratio below 100 GeV.

Not withstanding the above discussion, the “sensitivity” of a detector is a poorly defined concept. Since different astrophysical sources have different properties (energy spectrum, duration, prior knowledge of their existence) a single number called sensitivity is not useful. In what follows the sensitivity of HAWC to three
distinct phenomena is estimated: galactic sources with an energy spectrum of $E^{-2.49}$, active galaxies at various redshifts (to investigate the effect of the absorption of VHE photons by the extragalactic background light), and gamma ray bursts. The latter is a major motivation for this type of detector, since ACTs by their nature have no opportunity to the prompt phase of GRB emission.

1. Galactic Sources and Sky Survey

The Crab Nebula is the prototypical galactic TeV gamma ray source. In reality the spectrum of the Crab Nebula is not well represented by a power law over the energy range 10 GeV to 10 TeV. However, for simplicity and to enable a comparison to other instruments the spectrum of the Crab Nebula is assumed to be $dN/dE = 3.2 \times 10^{-7} E^{-2.4} \text{m}^{-2}\text{s}^{-1}$ over the energy range of HAWC. Using the procedure outlined above the number of detected gamma rays per source transit in HAWC is calculated. To estimate the background level in a bin of the same size with the same transit, the identical procedure is carried out with proton primaries (the criterion that the events must be reconstructed with 1.2 degrees of their true direction is dropped). The identical procedure is then performed for the Milagro Monte Carlo. The ratio of the simulated events observed in HAWC to the simulated events observed in Milagro is used to scale the background rate in HAWC. For an observation altitude of 5200m the background rate will be $\sim 85$ times that of Milagro and for an observation altitude of 4572m the background rate will be $\sim 60$ times larger than Milagro’s. These numbers apply to the raw data, before the application of any background rejection. Table I gives the expected number of source and background events for a single transit of the Crab. The predicted excess for Milagro is somewhat larger than is actually observed by Milagro. With two years of data Milagro observes roughly $4\sigma/\sqrt{\#\text{years}}$ on the Crab Nebula. The discrepancy is accounted for by three detector related effects (the dead-time in Milagro is about 12%, the on time is about 90%, and at any given time about 6% of the PMTs are not working) and one astrophysical effect, the spectrum of the Crab Nebula turns over at the higher energies. When these effects are properly accounted for the measurement of the Crab flux by Milagro is in good agreement with the measurement by HEGRA.

Table I shows that a detector at 5200m elevation is about 40% more sensitive than the same detector at 4572m elevation. This is in agreement with the results given above on the effect of altitude on the particles at the ground. But both elevations result in a detector that can observe the Crab Nebula at high significance in a single transit. This is an important feature which allows one to quickly verify all aspects of the detector response. Current ACTs such as the Whipple telescope obtain roughly 5$\sigma$ on the Crab Nebula in one hour of observation. Though the calculated transit here consists of 6 hours, the bulk of the signal arrives in a 4-hour span, so the sensitivity for the same observation period of HAWC will be roughly 1/2 that of the Whipple telescope. With one year of observation a 50 mCrab source would yield a 5$\sigma$ detection. In contrast the VERITAS 7-telescope array will detect a 7 mCrab source at 5$\sigma$ with a 50 hour observation. With this sensitivity level VERITAS would require 3-4 years of dedicated time to survey 2sr of the sky at the level of 50 mCrab. (This assumes no change in sensitivity for VERITAS for sources 1 degree off-axis.) It is worth noting that these two surveys are fundamentally different, in that HAWC would obtain a measurement (or upper limit) which is an average over a year, while the VERITAS measurement (or upper limit) would result from a 7-minute snapshot over a 3-4 year period. Given the transient nature of many VHE sources, such a snapshot may be a limited value. The gamma-ray rate (in HAWC) from the Crab will be roughly 0.4 Hz or 24/minute for a detector at 5200m and 0.23Hz (or 14/minute) for a detector at 4572m asl. This number compares favorably with VERITAS and is significantly higher than that currently observed by the Whipple telescope.

<table>
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<th>Bkgnd (Raw)</th>
<th>$\alpha$ (Raw)</th>
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<td>17</td>
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</table>

TABLE I: Expected Signals from the Crab Nebula in HAWC at 5200m and 4572m elevation. Milagro is at an elevation of 2700m and is $\sim 1/10$ the size of HAWC.
2. Extragalactic Sources

For more distant sources one must account for the absorption of high-energy photons caused by interactions with the extragalactic background light (EBL)\(^{13,16}\). While a direct measurement of the EBL has proved elusive, several models exist. In what follows the “fast evolution” model of Stecker and De Jager\(^{16}\) is used to estimate the effect as a function the redshift of the source on the sensitivity of HAWC. For nearby objects (redshift less than 0.05) there is a negligible difference between this model and the “baseline” model discussed in the reference. At a redshift of 0.2 the baseline model for the EBL results in \(\sim 15\%\) more signal events detected by HAWC than the model used here. Figure 14 shows the number of signal events detected as a function of energy for sources at various redshifts. Only events that satisfied the background rejection criterion, \(n_{\text{Top/PE}} > 4.3\), had more than 20 PMTs survive the angular reconstruction, and were reconstructed within 1.2 degrees of their true direction where used to calculate the curves in the figure. A source differential spectral index of -2.49 and an observation altitude of 5200m have been assumed in this figure. An integration of these curves gives the total number of detected events for each source.

![Figure 14: The estimated number of detected events in HAWC as a function of energy for a source with a differential spectral index of -2.49 placed at several different redshifts. An observation altitude of 5200m has been assumed in this figure.](image)

Using the modified spectra given in Figure 14 the sensitivity of HAWC to distant sources can be calculated. Figure 15 shows the number of days required to detect a source at the 5\(\sigma\) level as a function of source intensity for several different source redshifts. The source intensity is given in units of the Crab flux and is the flux that would be present at the top of the atmosphere if there was no absorption of the high-energy gamma rays. HAWC could detect a source at a redshift of 0.3 with a flux at the top of the atmosphere (before accounting for absorption) one tenth that of the Crab Nebula with less than one year of observation.

3. Gamma Ray Bursts

The study of the high-energy spectrum of gamma-ray bursts (GRBs) is perhaps the strongest motivation for an all-sky VHE telescope. While GLAST will have good sensitivity to GRBs up to several 10's of GeV, a ground-based instrument, with its much larger effective area, could have good sensitivity up to the highest energy gamma rays that reach the earth. The ability to study the prompt phase of VHE emission could lead to exciting new physics. Given its low energy threshold, HAWC would have sensitivity to GRBs at a redshift 1.

To estimate the sensitivity of HAWC to GRBs requires knowledge of any absorption at the source and the inevitable absorption of the VHE photons as they traverse the cosmos. Since one does not know the inherent spectrum of GRBs, in what follows the GRB energy spectrum is modeled as a power law with a sharp cutoff. This cutoff could arise from absorption at the source or from the EBL. By investigating the sensitivity of HAWC to different cutoff energies it is possible to estimate the sensitivity to GRBs at different redshifts. Figure 16 shows the sensitivity of HAWC (at an observation altitude of 4572m asl) to GRBs as a function of burst...
FIG. 15: The number of days required to detect a source at 5σ as a function of the source intensity for sources at various redshifts.

duration for several energy cutoffs. The spectra are assumed to be $E^{-2.4}$ up to the indicated cutoff energy, where the photon flux falls to zero. These curves give the flux level needed to observe a GRB at the 5σ level. No background rejection has been applied to these data. The black circles are data from the BATSE detector, giving the observed distribution of GRB fluence as a function of burst duration. The lower solid line is the sensitivity of GLAST and the upper solid line the sensitivity of EGRET. To detect a 1-second duration burst HAWC would require 50 events from a GRB over a background level of 85 events. The signal to noise level in a detected burst would be quite high.

FIG. 16: The sensitivity of HAWC to gamma-ray bursts. The dots are data points from BATSE observations of burst fluence as a function of burst duration. The lines show the required fluence to yield a 5σ detection in HAWC for various cutoff energies (as given in the legend). For comparison the sensitivities of EGRET and GLAST are shown.

Figure 16 can be used in conjunction with the known redshift distribution of GRBs and the known GRB rate to estimate how many GRBs/year HAWC would detect. Assuming that the intrinsic GRB spectrum extends to at least 50 GeV, one sees that roughly 20% of all GRB’s are bright enough to be detected by HAWC. If half of all bursts lie within a redshift of 1 and assuming a GRB rate of 1 per day, HAWC (which views 1/6 of the sky) would detect at least 6 GRBs per year. If the intrinsic GRB spectra extend beyond 50 GeV HAWC would detect more bursts.
V. CONCLUSIONS

A design for the next generation all-sky VHE gamma-ray telescope has been presented. This instrument, HAWC, would be over 20 times more sensitive than the Milagro detector. With the ability to continuously view the entire overhead sky HAWC will be an excellent complement to both GLAST and the coming generation of air Cherenkov telescopes (HESS, MAGIC, VERITAS, and CANGAROO III). With comparable sensitivity to GLAST it will be the only instrument capable of monitoring the many thousands of sources that GLAST is expected to detect at higher energies. In addition to searching the sky for galactic sources (the VHE complement to the 150 EGRET unidentified objects), and active galaxies, the low-energy sensitivity of a detector placed at high altitude ensures that such an instrument will detect any VHE emission from gamma-ray bursts. Perhaps most importantly an open apertures instrument with this level of sensitivity could discover completely new and unexpected phenomena that have so far eluded detection.